Performance Analysis of Concurrent Red-Black Trees on HTM Platforms

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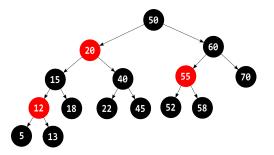
- Hardware Transactional Memory (HTM) support on modern processors:
 - IBM Power8, Blue Gene/Q, zEC12.
 - Intel Haswell, Broadwell ...
- We need to evaluate its performance with real life applications.

Red-Black trees:

- Widely used for dictionary implementations.
- Challenging to devise efficient concurrent implementations(e.g. with locks or atomic primitive).
- Their properties favor the usage of HTM.

Red-Black Trees

Red-Black Trees in a nutshell



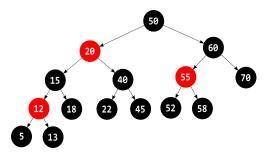
Definition

Binary Search Tree (BST) with the following additional properties:

- A node is either black or red.
- 2 The root is black.
- 3 All leaves are black.
- Every red node must have two black children.
- Severy path from a given node to any of its descendant leaves contains the same number of **black** nodes.

The above properties guarantee that the tree is almost balanced.

Red-Black Trees in a nutshell



Applications

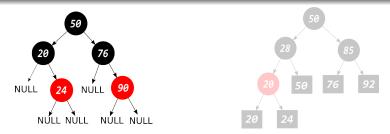
Dictionary ADT:

• Colection of (key, value) pairs.

Supports three operations:

- Lookup
- Insert
- Delete

Internal VS External RBTs



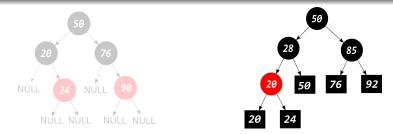
Internal:

• Both keys and values are stored in every node.

External:

- Values are stored only in the leaves.
- Internal nodes are only used for routing purposes.
- Occupy more memory.
- + Simplify delete operation.
- All our implementations are external trees.

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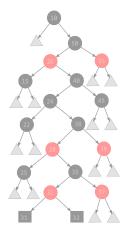
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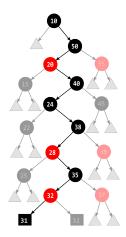
Example: lookup(31)

- Just like in BST.



Serial:

- Just like in BST.
- Traverse the tree from the root to the appropriate leaf.
- Lookups always reach a leaf (external tree).

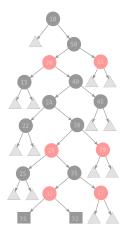


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Fine-grained locking:

- Hand-over-hand locking.
- Lock next node before releasing current.

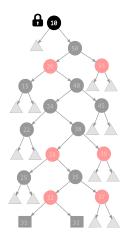


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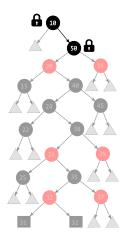


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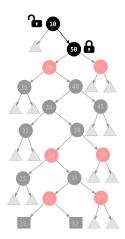


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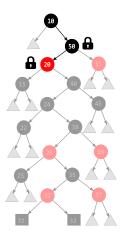


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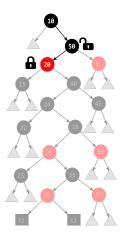


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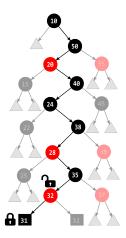


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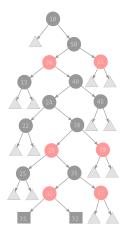
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Coarse-grained HTM:

- Read-only transaction.
- Transactional read-set consists of the traversed nodes.



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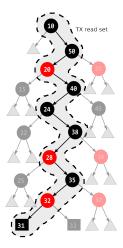
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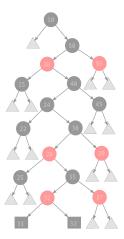
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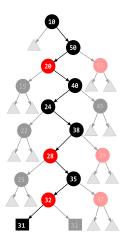


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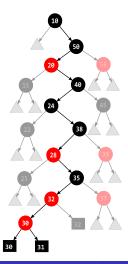


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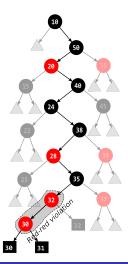
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Bottom-up ^[1]:

- Traverse the tree from the root to the appropriate leaf.
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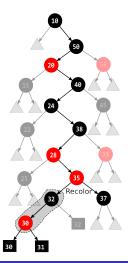
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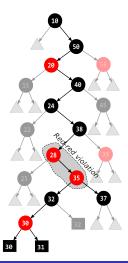
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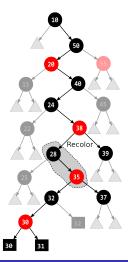
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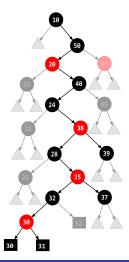
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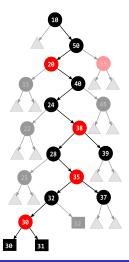
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- Top-down approach performs insertion in one pass.

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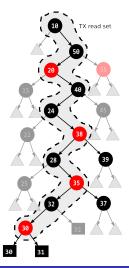
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- Transactional read-set consists of the traversed nodes plus nodes accessed in fixup phase.
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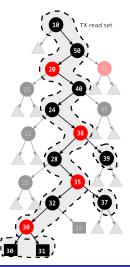
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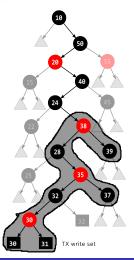
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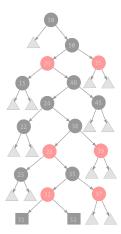
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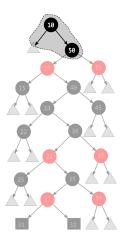


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- Traverse the tree recoloring/rotating nodes.

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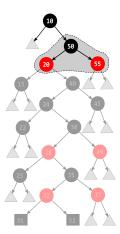


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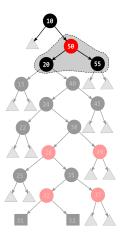


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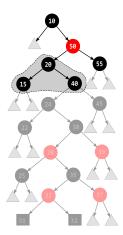


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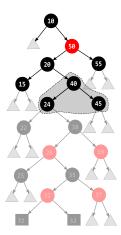


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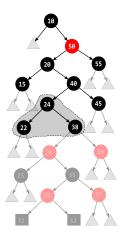


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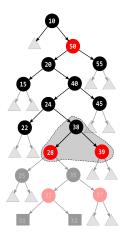


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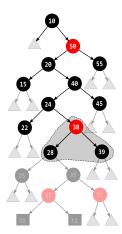


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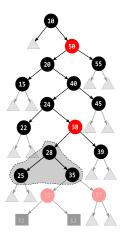


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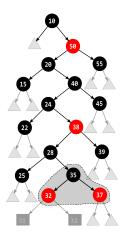


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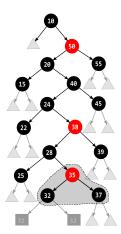


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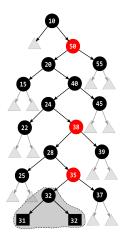


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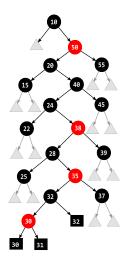


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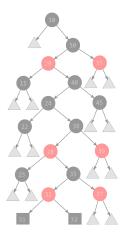
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Fine-grained locking:

- All threads traverse the tree in one direction.
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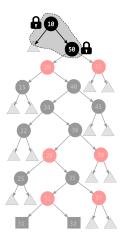
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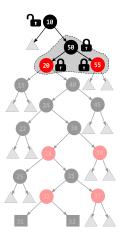
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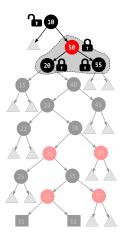
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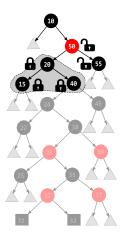
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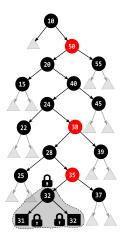
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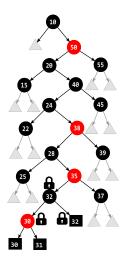
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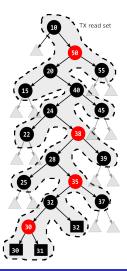
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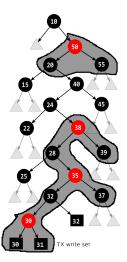
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Bottom-up:

- Traverse the path to the appropriate node.
- Delete the node.
- Fixup the violation.
 - Similar to bottom-up insertion.
 - Recolors propagate the violation and, if necessary, 1 2 or 3 rotations

Top-down:

- One top-down pass.
- Recolors/rotations while traversing the tree to assure no reverse traversal is necessary.

Concurrent red-black tree implementations

| | Bottom-up | Top-down |
|---------------------|------------|------------|
| Coarse-grained lock | bu_cg_lock | - |
| Fine-grained lock | - | td_fg_lock |
| Coarse-grained HTM | bu_cg_htm | td_cg_htm |

HTM

Current HTM platforms

| | Intel Haswell | IBM Power8 |
|----------------------|---------------|----------------------------|
| Versioning | Lazy | |
| Progress guarantees | Best effort | |
| Conflict detection | Eager | |
| Conflict granularity | Cache line | |
| Cache line size | 64KB | 128KB |
| TX read-set | 4MB | 8KB |
| TX write-set | 22KB | 8KB |
| Failure reasons | Conflict | Transactional conflict |
| | | Non-transactional conflict |
| | Capacity | |
| | Explicit | |

Experimental Evaluation

| Name | Haswell | Power8 |
|------------|--|---|
| Processors | 1 × Intel Core i7-4771 | 2 x Power8 |
| # Cores | 4 | 2 × 10 |
| # Threads | 8 | 160 |
| Core clock | 3.5 GHz | 3.7 GHz |
| L1 (Data) | 8-way, 32 KB, 64B block size | 8-way, 64 KB, 128B block size |
| L2 | 8-way, 256 KB, 64B block size | 8-way, 512 KB, 128B block size |
| L3 | 16-way, 8 MB, 64B block size (shared) | 8-way, 80 MB, 128B block size (shared per die) |
| Memory | 16 GB | 256 GB |

Experimental Setup

Code

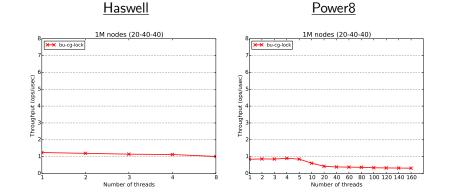
- Written in C.
- GCC 4.9.1, -O3 optimization flag used.
- Nodes are padded to fit in one cache line.

HTM Evaluation

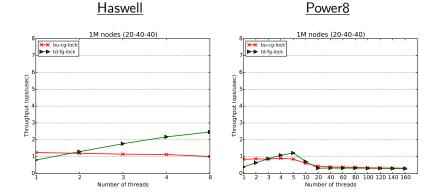
- Tree sizes (5 configurations):
 - Small: 1K nodes \rightarrow 9-12 nodes in paths, \approx 250KB.
 - Large: 10M nodes \rightarrow 19-29 nodes in paths, \approx 2.5GB.
- Operations workload (%lookups-%insertions-%deletions):
 - Read-intensive: 80-10-10
 - Read-write: 50-25-25
 - Write-intensive: 20-40-40

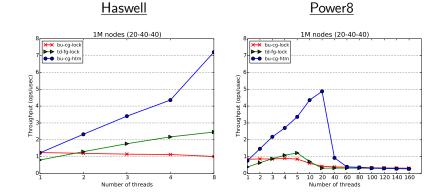
Benchmarks Execution

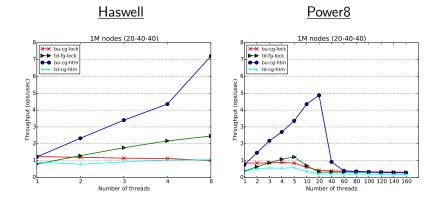
- Employ empty physical cores before SMT contexts.
- RTM mode only in Haswell.
- 10M operations equally divided between threads.
- Warmup phase to initialize the tree with half of the possible keys.
- 10 transactional retries before acquiring the global lock.



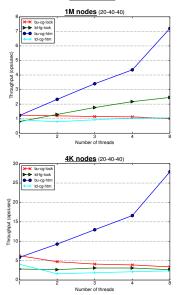
Haswell



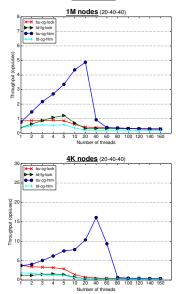


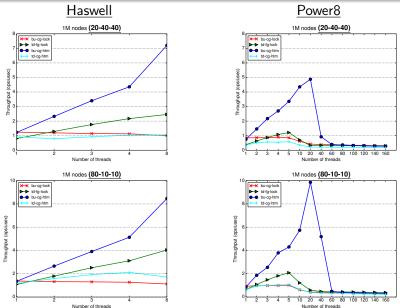


Haswell

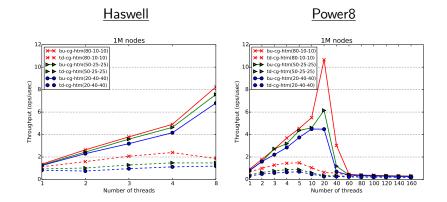


Power8

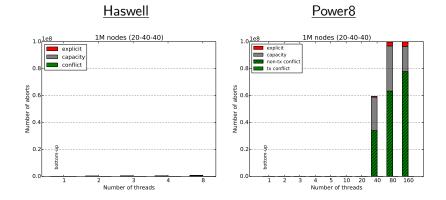




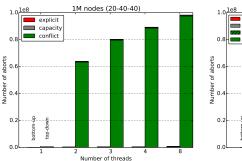
Evaluation: HTM Bottom-up VS Top-down



Evaluation: HTM Bottom-up VS Top-down

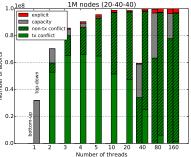


Evaluation: HTM Bottom-up VS Top-down

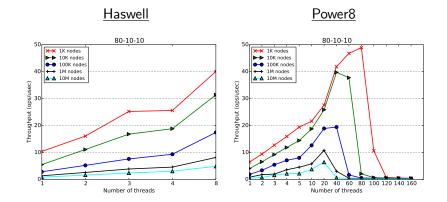


Haswell





Evaluation: Effects of HTM imposed limits



- HTM:
 - Better than fine-grained locking ...
 - ... with programming effort similar to coarse-grained locking.
- Hardware imposes performance limits.
 - More intense when resourses are shared.

Future Directions

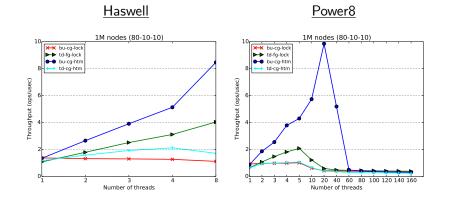
- Cpu_lock fallback
- Hand-over-hand transactions
- $\bullet\,$ More data structures, e.g. AVL trees, B+ trees ...
- ... any suggestions?

Preliminary results on my lightning talk :)

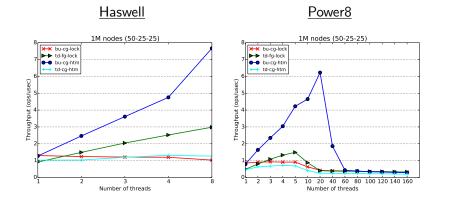
Thank you for your attention! Questions?

Backup

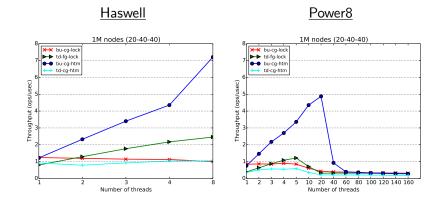
HTM VS Locks: 1M nodes (80-10-10)



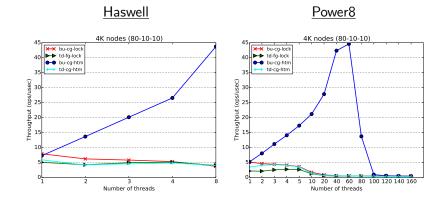
HTM VS Locks: 1M nodes (50-25-25)



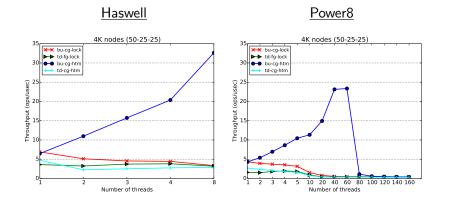
HTM VS Locks: 1M nodes (20-40-40)



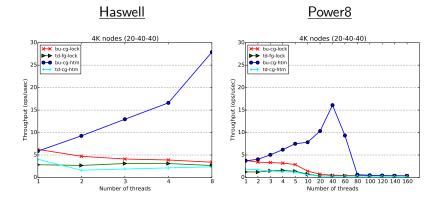
HTM VS Locks: 4K nodes (80-10-10)



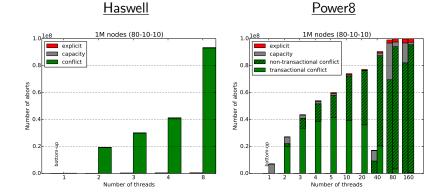
HTM VS Locks: 4K nodes (50-25-25)



HTM VS Locks: 4K nodes (20-40-40)

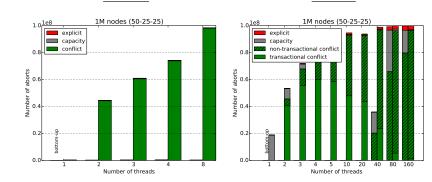


Bottom-up VS Top-down: 1M nodes (80-10-10)



Bottom-up VS Top-down: 1M nodes (50-25-25)

Haswell



Power8

Bottom-up VS Top-down: 1M nodes (20-40-40)

1.0<u>1</u>e8 1M nodes (20-40-40) 1M nodes (20-40-40) 1 explicit explicit capacity capacity conflict non-transactional conflict 0.8 0.8 transactional conflict Number of aborts Number of aborts 0.6 0.6 0 0 0.2 0.2 0.0 0.0 3 5 10 20 1 4 8 2 3 4 Number of threads Number of threads

Haswell

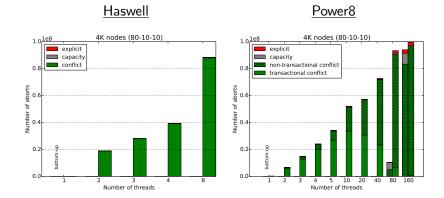
Power8

80

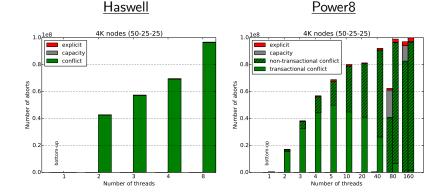
160

40

Bottom-up VS Top-down: 4K nodes (80-10-10)



Bottom-up VS Top-down: 4K nodes (50-25-25)



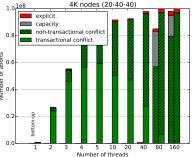
TRANSACT' 15

Bottom-up VS Top-down: 4K nodes (20-40-40)

1.0<u>1</u>e8 4K nodes (20-40-40) 1e8 1.0 explicit explicit capacity capacity conflict 0.8 0.8 Number of aborts Number of aborts 0.6 0.6 0 0.2 0.2 0.0 0.0 3 1 4 8 Number of threads

Haswell

Power8



Haswell VS Power8 single threaded performance

• Bottom-up serial, 80-10-10 workload.

| Tree Size (Nodes) | Haswell Power8 | |
|----------------------|----------------|------|
| 1К | 11.82 | 6.82 |
| 1M | 1.38 | 0.97 |
| 10M | 0.86 | 0.53 |

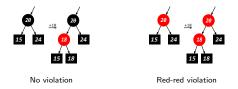
Table : Single thread throughput (ops/usec).

Number of recolors per fixup operation

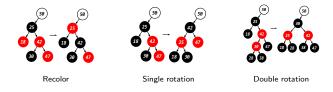
| Recolors | Nodes | | | |
|----------|--------|--------|--------|--------|
| | 2M | 20M | 100M | 200M |
| 0 | 77.12% | 75.96% | 73.37% | 73.08% |
| 1 | 19.52% | 18.66% | 18.73% | 18.79% |
| 2 | 2.78% | 3.69% | 5.30% | 5.47% |
| >2 | 0.56% | 1.69% | 2.59% | 2.66% |

Table : Distribution of fix-ups based on performed recolors.

• When the newly inserted node's parent is red, a red-red violation is created:

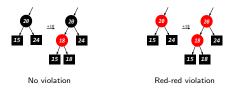


• When a violation is created a fixup is required:



Deletion

• When the removed internal node is black the path becomes short:



• When a violation is created a fixup is required:

